

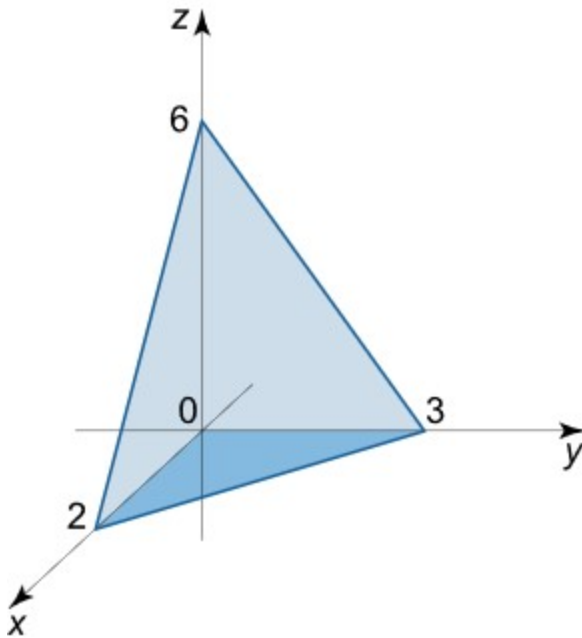
Chapter - 1

Practice problems

(1) Evaluate the integral $\int_0^2 \int_0^z \int_0^y xyz dx dy dz$

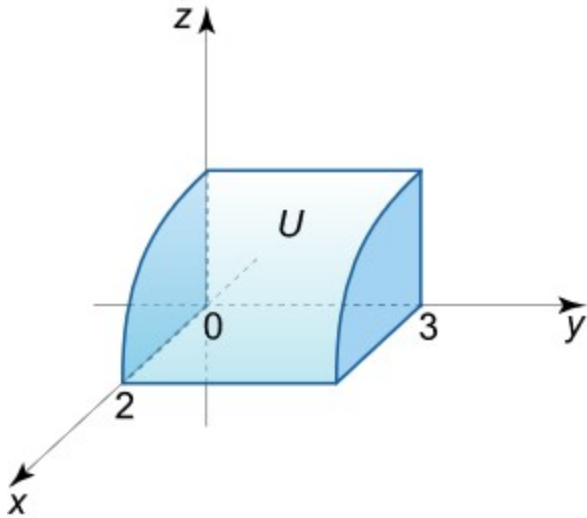
Ans: $4/3$

(2) Evaluate the integral $\iiint (1 - x) dx dy dz$ in first octant below the plane $3x + 2y + z = 6$



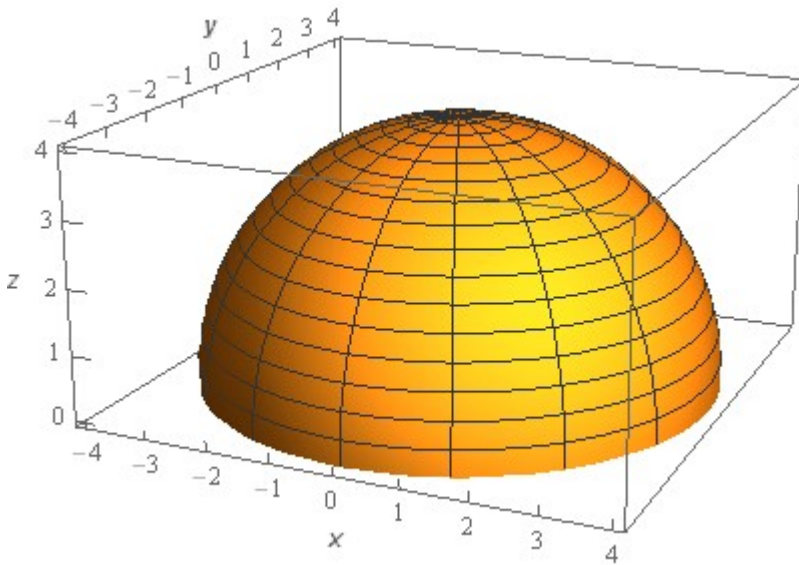
Ans: 3

(3) Evaluate the volume of a cylinder represented by $x^2 + z^2 = 4$ in the first octant bounded by the plane $y = 3$. Do this in Cartesian and cylindrical co-ordinate system.



Ans: 3π

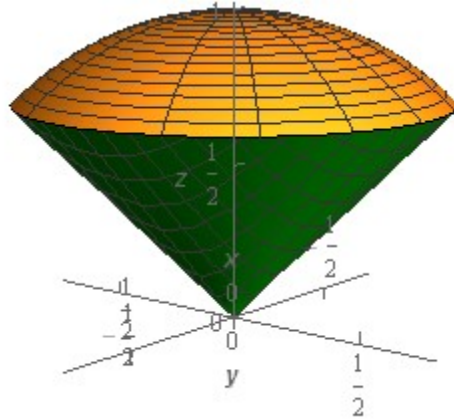
(4) Evaluate $\iiint (10xz + 3)dV$ where the region is defined by the equation $x^2 + y^2 + z^2 = 16$ with $z \geq 0$.



Ans: 128π

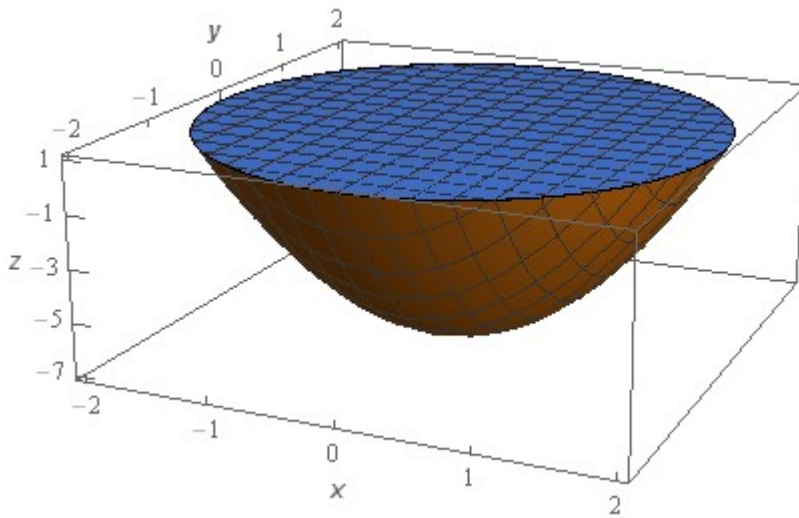
(5) Evaluate volume of an ice-cream cone defined by the volume enclosed by the surfaces

$$x^2 + y^2 + z^2 = 1 \text{ and } z = \sqrt{x^2 + y^2}.$$



Ans: $\frac{2\pi}{3} \times 0.292$

(6) Evaluate $\iiint 4xydV$ inside a volume bounded by $z = 2x^2 + 2y^2 - 7$ and $Z = 1$.



Ans: 0